

DAN'S ONE-DAY CALCULUS LECTURE

Prerequisites

Slope, area, functions, inverses.

Derivatives

The slope at any point of a function. Symbol: $f'(x)$

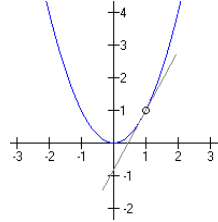
Ex.: Let $f(x) = x^2$. Graph this.

(Like a roller coaster-track; use eraser as car.)

Q: At each x-value, what is the slope?

x	-2	-1	0	1	2
slope	-4	-2	0	2	4

So: $f'(x) = 2x$



Integrals

The area up to a given point of a function. Symbol: $\int f(x)$

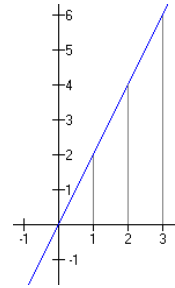
Ex.: Let $f(x) = 2x$. Graph this.

(Growing business income, or drag racer velocity/distance.)

Q: At each x-value, what is the area? ($A = \frac{1}{2}lw$)

x	0	1	2	3
area	0	1	4	9

So: $\int f(x) = x^2$.



Fundamental Theorem of Calculus

Derivatives (slopes) and integrals (areas) are inverses.

More Detail

- (1) Precisely calculate slopes instead of guessing them (using "limit" concept)
- (2) Quickly calculate slope & integral functions instead of graphing points.